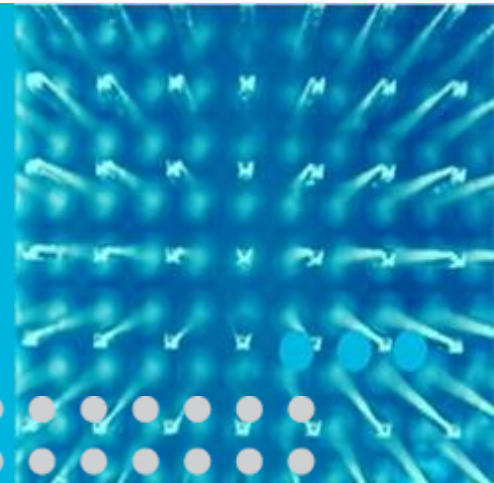


# Scaling Properties of Delay Tolerant Networks with Correlated Motion Patterns



Uichin Lee, Bell Labs/Alcatel-Lucent

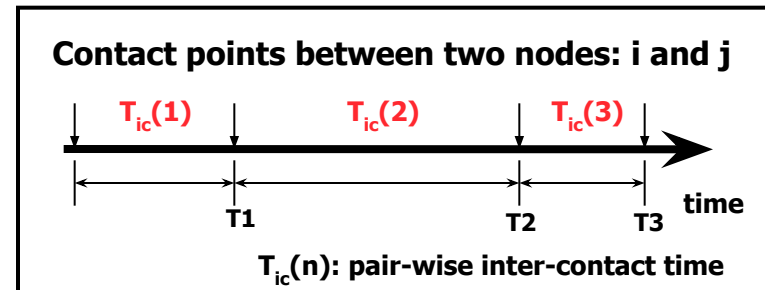
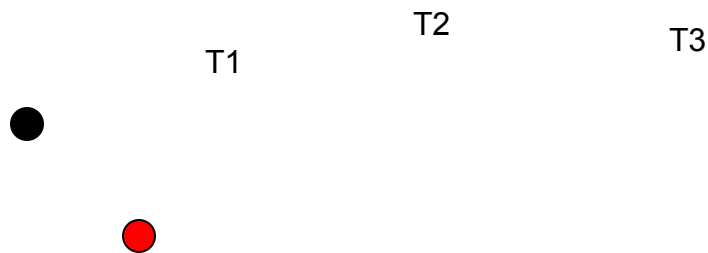
Soon Y. Oh, Mario Gerla (UCLA)

Kang-Won Lee (IBM T.J. Watson Research)

# Key DTN Metric: Pair-wise Inter-contact Time

Key metric for measuring *end-to-end delay*

Pair-wise inter-contact time: interval between two contact points

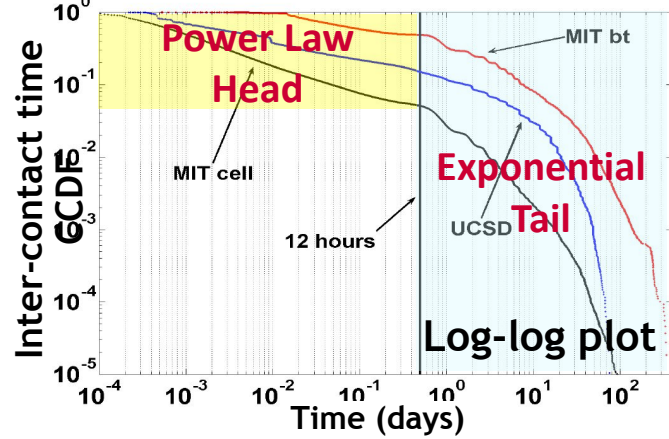
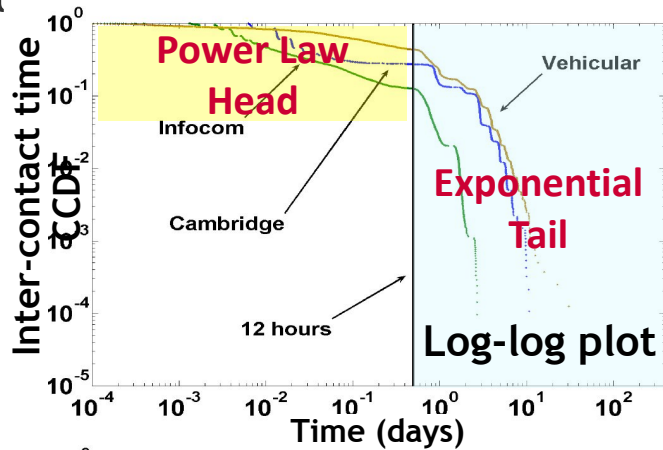


Inter-contact distribution:

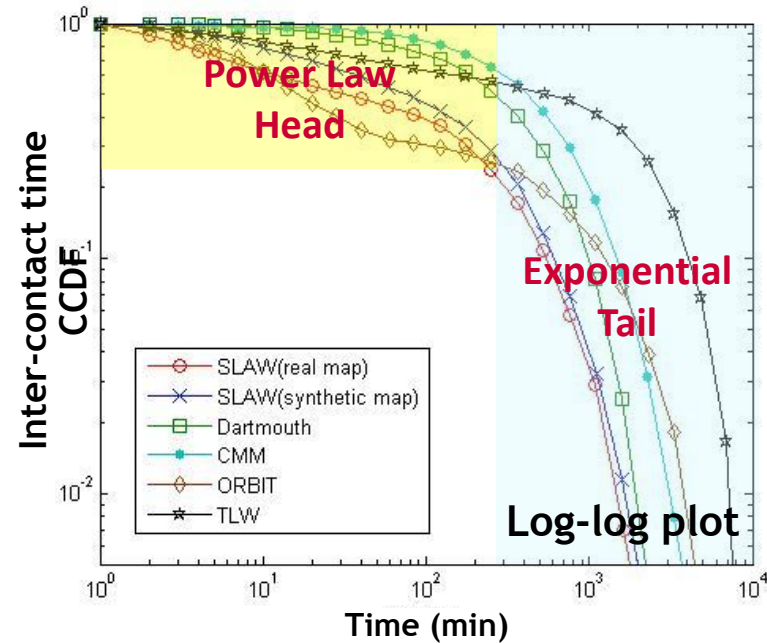
- Exponential 😊: bounded delay, but not realistic?
- Power-law 😞: may cause infinite delay, but more realistic?

# Two-phase Inter-contact Time

Two-phase distribution: power-law head and exponential tail



Karagiannis et al., MobiCom'07



Levy walk based mobility  
Lee et al. Infocom'08/09

- Association times w/ AP (UCSD) or cell tower (MIT cell)
- Direct contact traces: Infocom, cambridge (imotes), MIT-bt

# Two-phase Inter-contact Time

Why two-phase distribution? One possible cause:

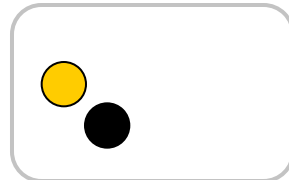
- Flight distance of each random trip (within a finite area) [Cai08]
- The shorter the flight distance, the higher the motion correlation in local area, resulting heavier power-law head
  - Power-law head while in local area vs. exponential tail for future encounters

**Goal: understand patterns on**

each other; and

- Levy flight of
- Vehicular mobility
- High correlation
- After leaving

Frequent encounters in local area



*Local area*

**Restricted motion  
and long properties**

occasional long flights  
(traffic jam)

“night”

\*Cai08: Han Cai and Do Young Eun, Toward Stochastic Anatomy of Inter-meeting Time Distribution under General Mobility Models, MobiHoc'08

\*Rhee08: Injong Rhee, Minsu Shin, Seongik Hong, Kyunghan Lee and Song Chong, On the Levy-walk Nature of Human Mobility, INFOCOM'08

# DTN Model: *Inter-contact rate + flight distance*

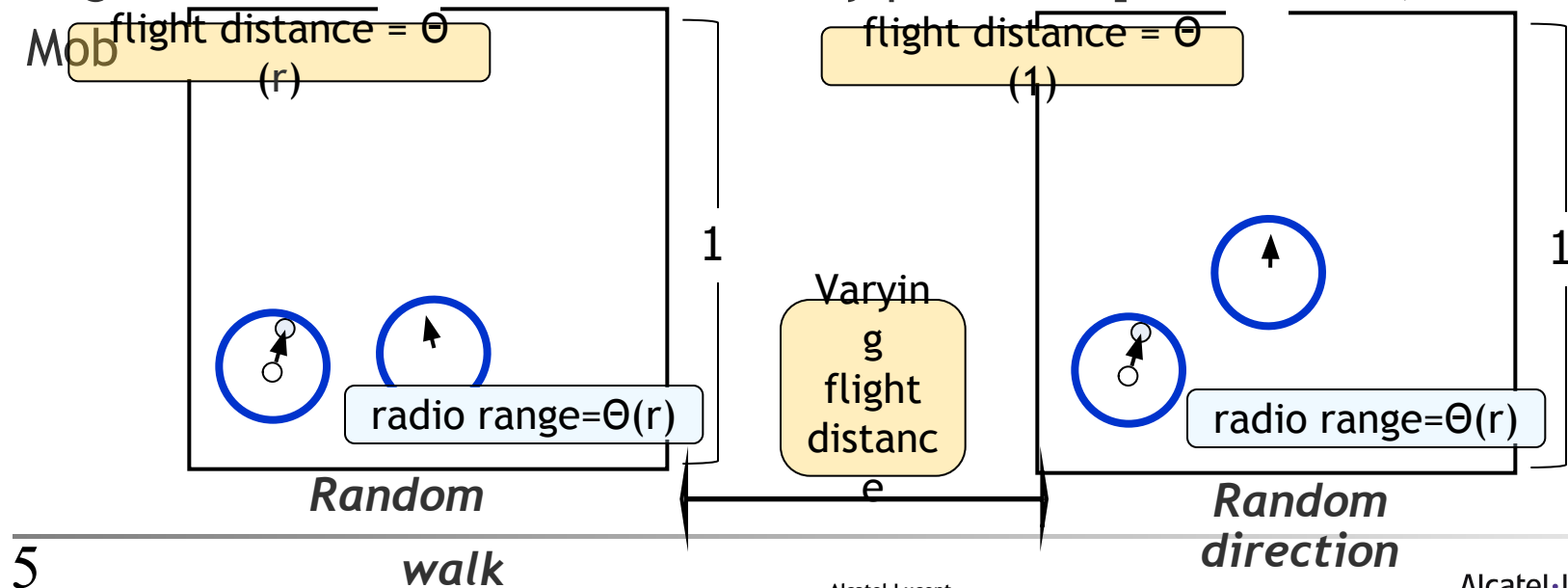
**Inter-contact rate:**  $\lambda \sim \text{speed } (v) * \text{radio range } (r)$  [Groenevelt, Perf'05]

- Random waypoint/direction (exp inter-contact time)

**Flight distance (motion correlation):**

- Ranging from radio radius  $\Omega(r)$  to network width  $O(1)$

**Invariance property:** avg inter-contact time does not depend on the degree of correlation in the mobility patterns [Cai et al, Eun,

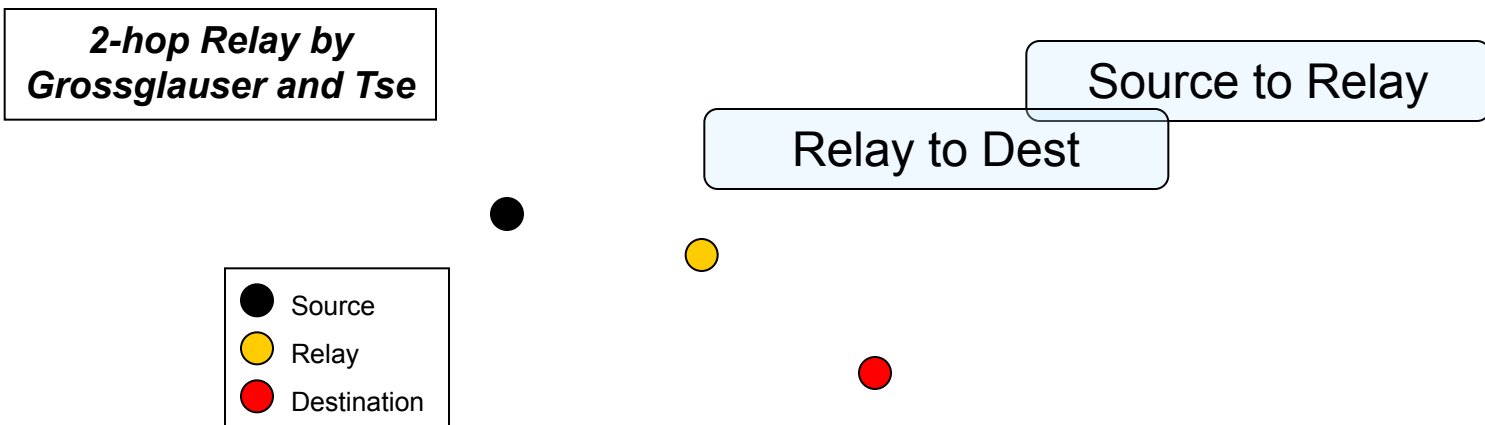


# 2-Hop Relay: DTN Routing

Each source has a random destination (n source-destination pairs)

**2-hop relay protocol:**

1. Source sends a packet to a relay node
2. Relay node delivers a packet to the corresponding receiver



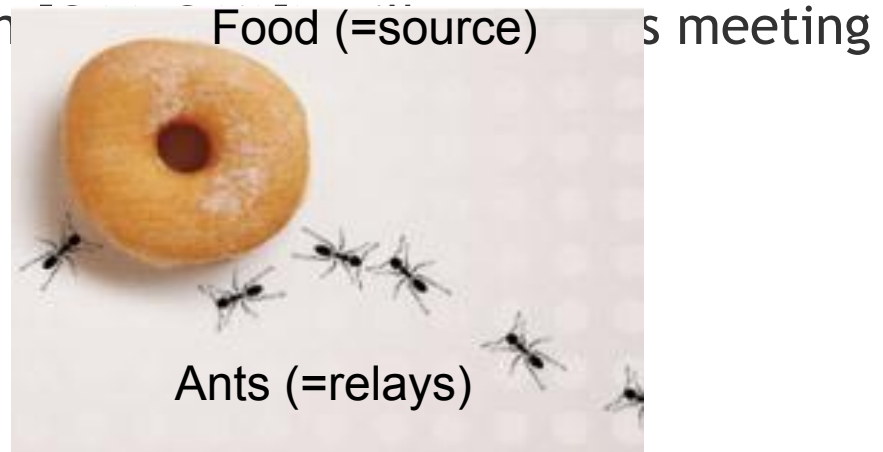
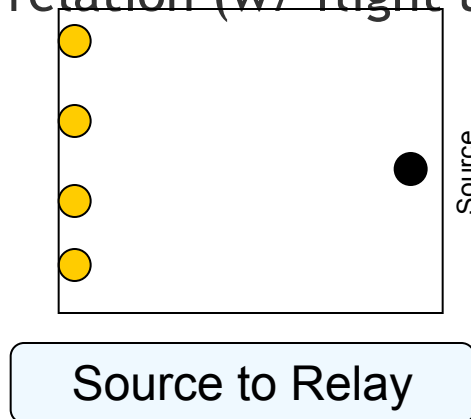
# 2-Hop Relay: Throughput Analysis

Intuition: avg throughput is determined by aggregate meeting rate (src  $\leftrightarrow$  relay and relay  $\leftrightarrow$  dest)

Two-hop relay per node throughput :  $\Theta(n\lambda)$

- Aggregate meeting rate at a destination:  $n\lambda$
- Grossglauser and Tse's results:  $\Theta(n\lambda)=\Theta(1)$  when  $\lambda = 1/n$  (i.e., speed  $1/\sqrt{n}$ , radio range  $1/\sqrt{n}$ )

Motion correlation (w/ flight length) is meeting rate



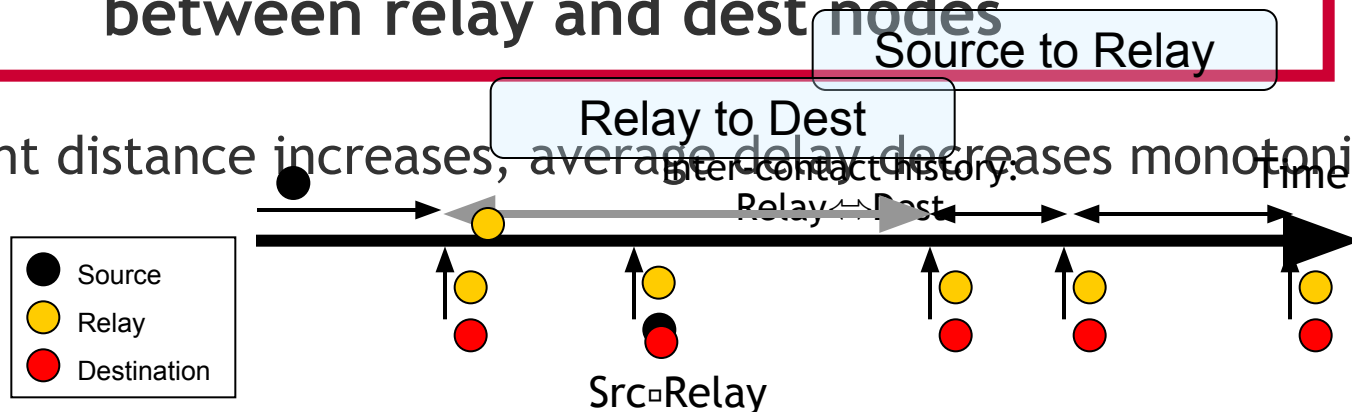
# 2-Hop Relay: Delay Analysis

Source to relay node ( $D_{sr}$ ), and then relay to dest ( $D_{rd}$ )

- $D_{sr}$  = avg. inter-any-contact time to a random relay
- $D_{rd}$  = avg. residual inter-contact time (relay  $\leftrightarrow$  dest)
  - Mean residual inter-contact time ( $D_{rd}$ ) =  $E[T^2] / 2E[T]$
  - >> T is a random variable for inter-contact time

**Inspection paradox (length bias): source tends to sample a longer inter-contact interval between relay and dest nodes**

- As flight distance increases, average delay decreases monotonically





# 2-Hop Relay: Buffer Requirement

Little's law: buffer = (rate) x (delay)

Required buffer space per node:  $B = [\Theta(n), \Theta(n \log n)]$

- Rate\*delay =  $\Theta(n\lambda) * [1/\lambda, \log n/\lambda] = [\Theta(n), \Theta(n \log n)]$

- Recall: random direction ( $1/\lambda$ ) and random walk ( $\log n/\lambda$ )

- Motion correlation

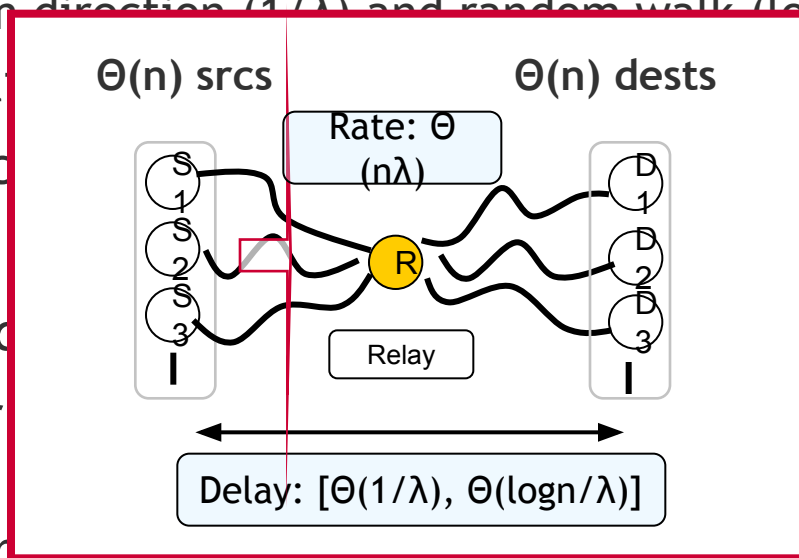
- Correlation inc

Impact of limited

- Limited buffer sources

- Relay node carries a packet to a certain dest with prob.  $K/B$

- Throughput per source =  $\Theta(n\lambda * K/B)$



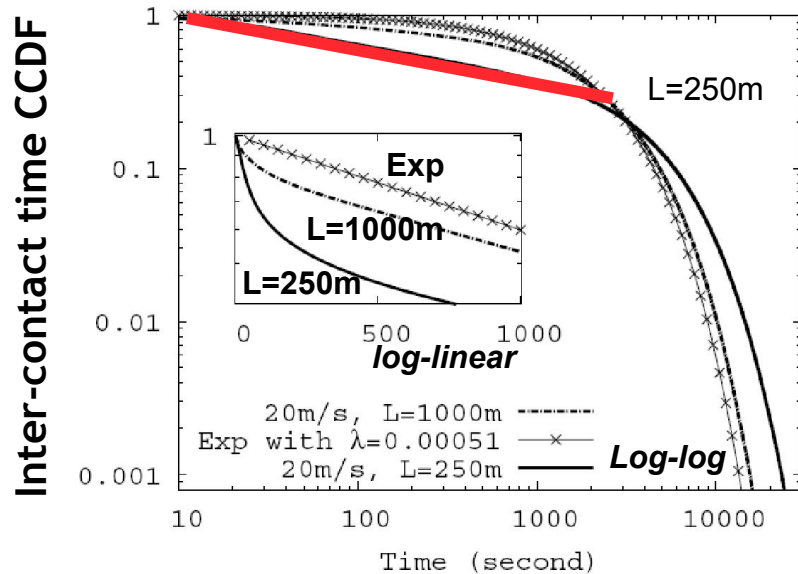
by shared by *all*

# Simulation: Throughput

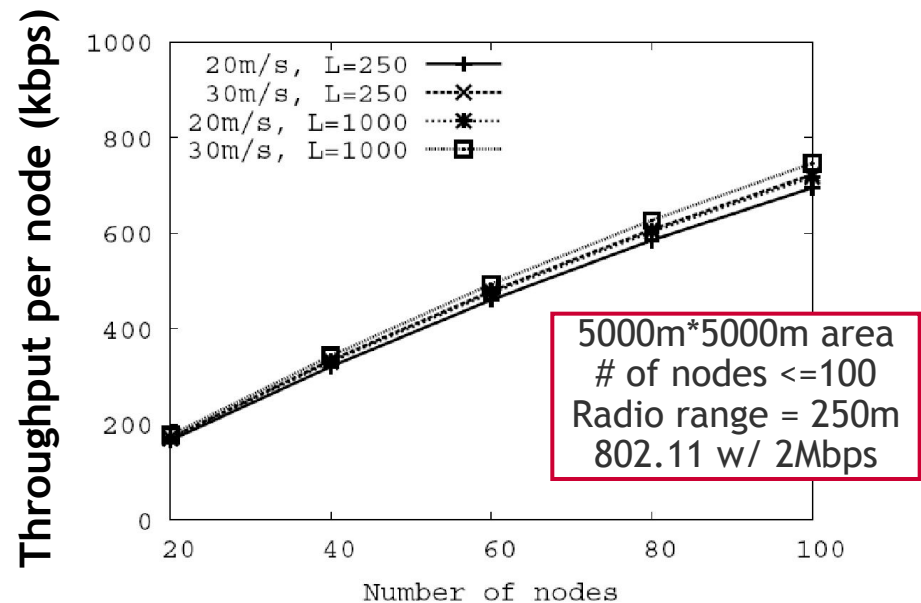
Degree of correlation via average flight distance  $L$

- $L=250\text{m}$  □ high correlation  $\Leftrightarrow$  power law head + exponential tail
- $L=1000\text{m}$  □ low correlation  $\Leftrightarrow$  almost exponential

Throughput is independent of the degree of correlations



CCDF of inter-contact time (20m/s)



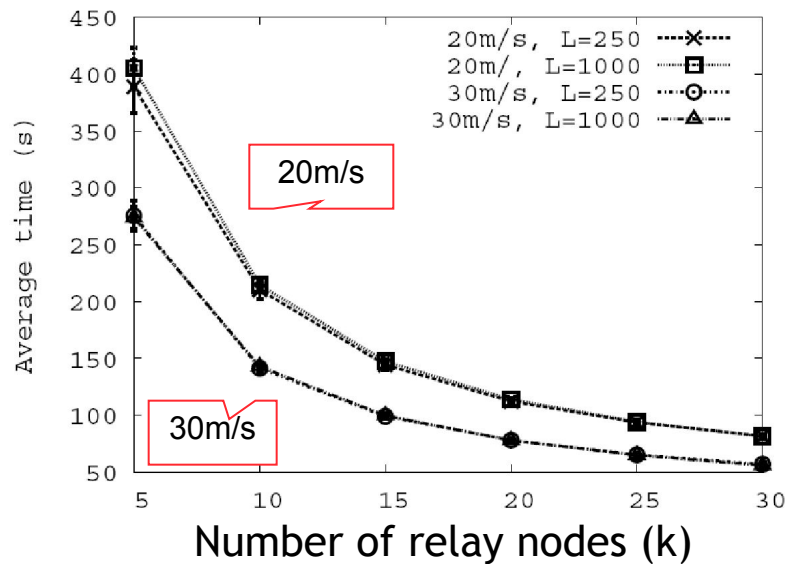
Average throughput per node as a function of # nodes

# Simulation: Inter-any-contact Time

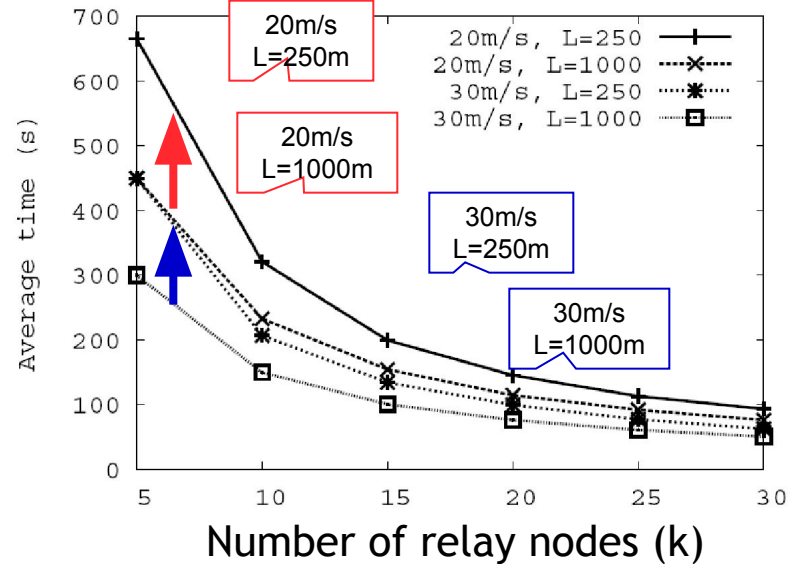
Inter-any( $k$ )-contact time: inter-contact time to *any of  $k$  nodes*

Invariance property: avg inter-contact time is independent of correlation

Residual inter-contact time: source probes a random point of the inter-meeting times between relay and destination



Average Inter-contact time

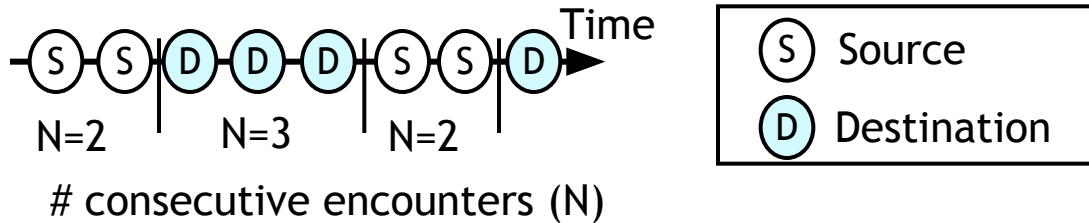


Average residual inter-contact time

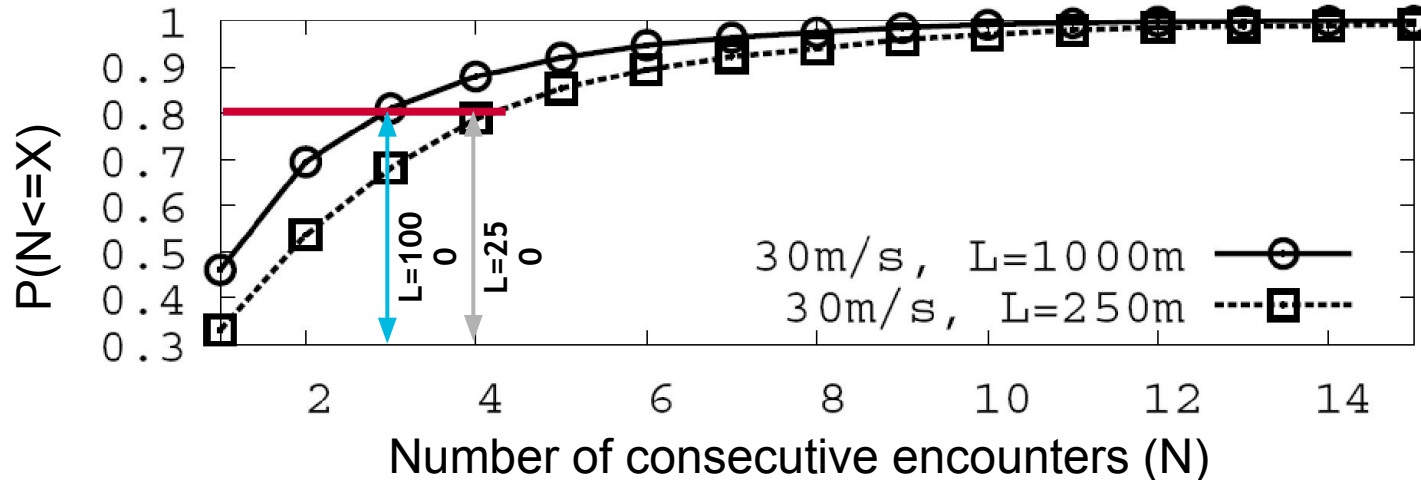
# Simulation: Buffer Utilization

Burstiness of relay traffic increases with the degree of correlation

*Relay node's contact history*



**Cumulative dist of # consecutive encounters**



# Conclusion

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Impact of correlated motion patterns on DTN scaling properties

DTN model: inter-contact rate + motion correlation via flight distance

- Flight distance of  $\Omega(r)$ ; i.e., min travel distance  $\sim$  one's radio range
- Considered mobility ranges from Random Walk to Random Direction

Main results:

- Throughput is independent of motion correlation
- Delay monotonically increases with the degree of correlation
- Buffer requirement also increases with the degree of correlation
- Correlation increases burstiness of relay traffic

Future work:

- Applying results to DTN multicast scenarios
- Scaling properties of inter-domain DTN scenarios